Quantity	Definition or Expression	Excel Function
<b>mean</b> — your best guess for the quantity you measured	$\bar{y} = \frac{1}{N} \sum_{n=1}^{N} y_n$	=AVERAGE()
<b>standard deviation</b> — a measure of the width of the distribution of your data points	$\sigma_y = \left[\frac{1}{N-1} \sum_{n=1}^{N} (y_n - \bar{y})^2\right]^{1/2}$	=STDEV()
<b>standard deviation of the mean</b> (aka standard error) — your best guess for the <i>random</i> uncertainty of the measurement	$\sigma_{\bar{y}} = \frac{\sigma_y}{\sqrt{N}}$	=STDEV()/ SQRT(COUNT())
weighted average — this is how to combine several measurements of the same thing that have different uncertainties	$\bar{x} = \frac{\sum_i x_i / \sigma_i^2}{\sum_i 1 / \sigma_i^2}  \sigma = \left[\sum_i 1 / \sigma_i^2\right]^{-1/2}$	
Error Propagation		
general uncorrelated errors $z = z(x, y)$	$\delta z = \left[ \left( \frac{\partial z}{\partial x}  \delta x \right)^2 + \left( \frac{\partial z}{\partial y}  \delta y \right)^2 \right]^{1/2}$	
sum $z = x + y$	$\delta z = \sqrt{(\delta x)^2 + (\delta y)^2}$	
product $z = xy$	$\frac{\delta z}{z} = \left[ \left( \frac{\delta x}{x} \right)^2 + \left( \frac{\delta y}{y} \right)^2 \right]^{1/2}$	
generalized product $z = x^m y^n$	$\frac{\delta z}{z} = \sqrt{\left(m\frac{\delta x}{x}\right)^2 + \left(n\frac{\delta y}{y}\right)^2}$	

## **Plotting and Analyzing Results**



• *Do they appear random?* Are about 2/3 of the points within one error bar from the

- Does the curve describe the data
- Are the parameter values
- Is the reduced value of  $\chi^2$ approximately equal to 1?