

*Today:* Introduction  
Coordinate Systems  
Transformations  
Astrometry

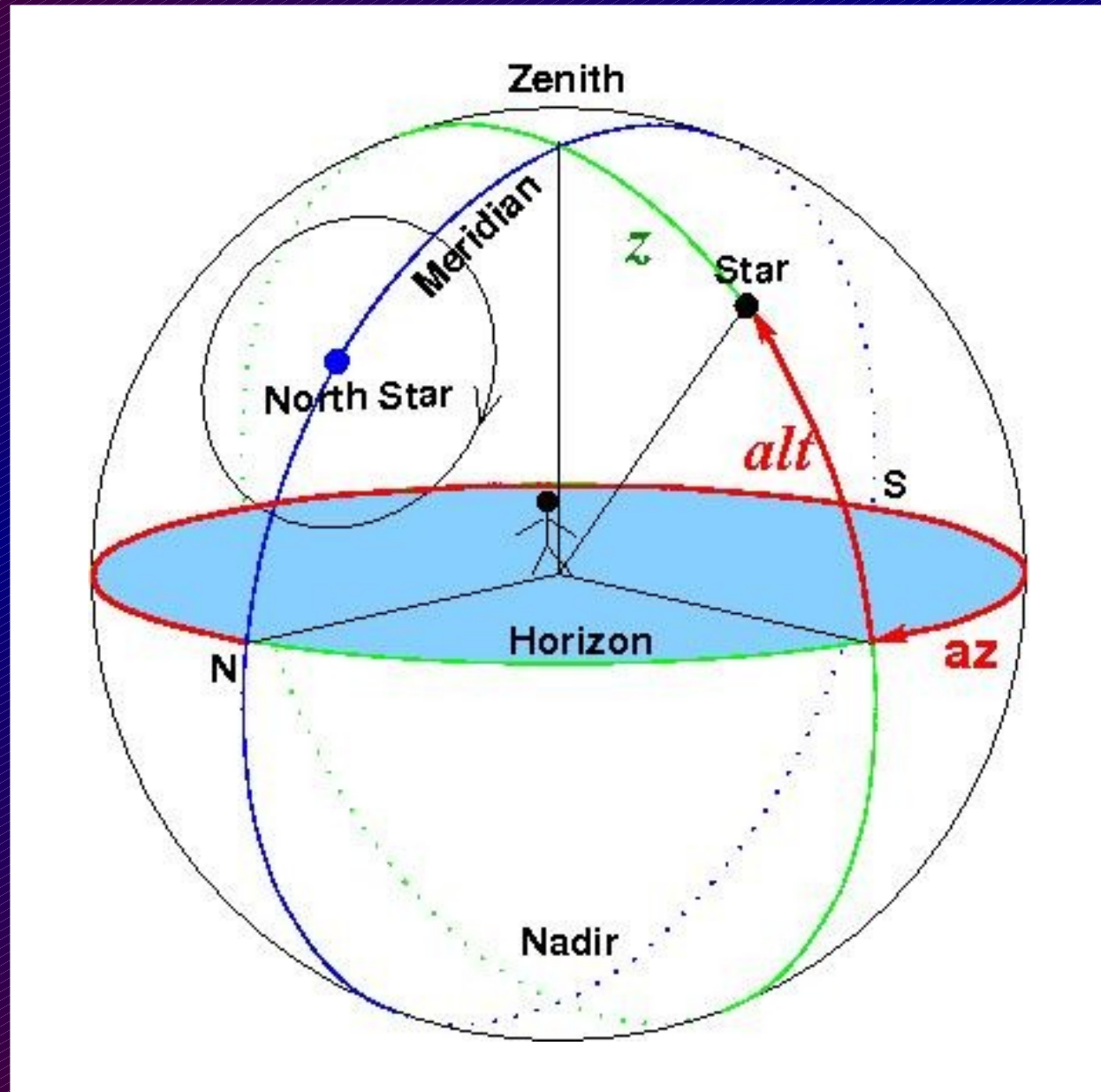
*Reading: Ch. 1, 4*

# Altitude – Azimuth Coordinate System

$alt (a) = \text{altitude}$

$az (A) = \text{azimuth}$

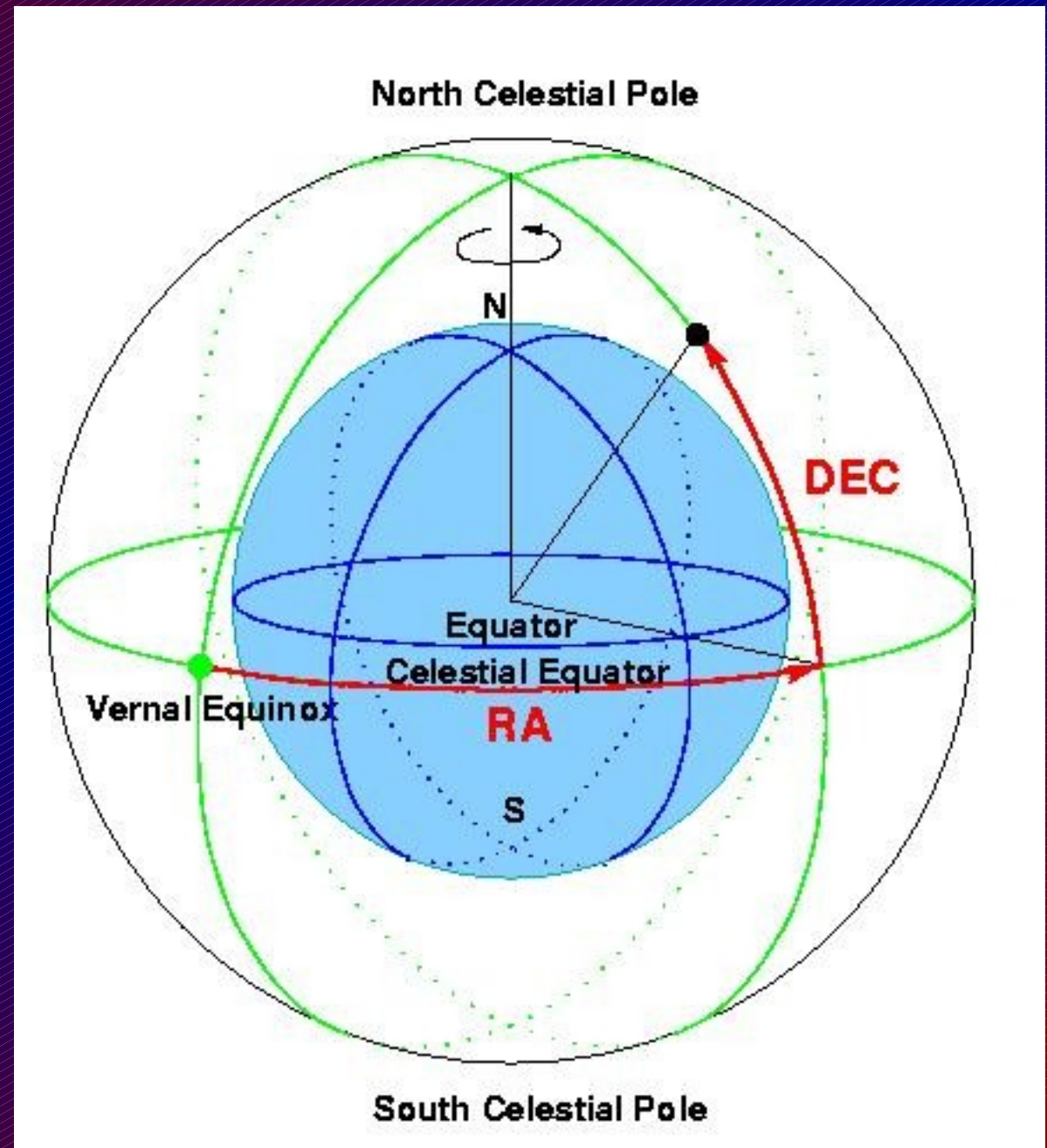
$z = 90^\circ - a$   
 $= \text{zenith distance}$



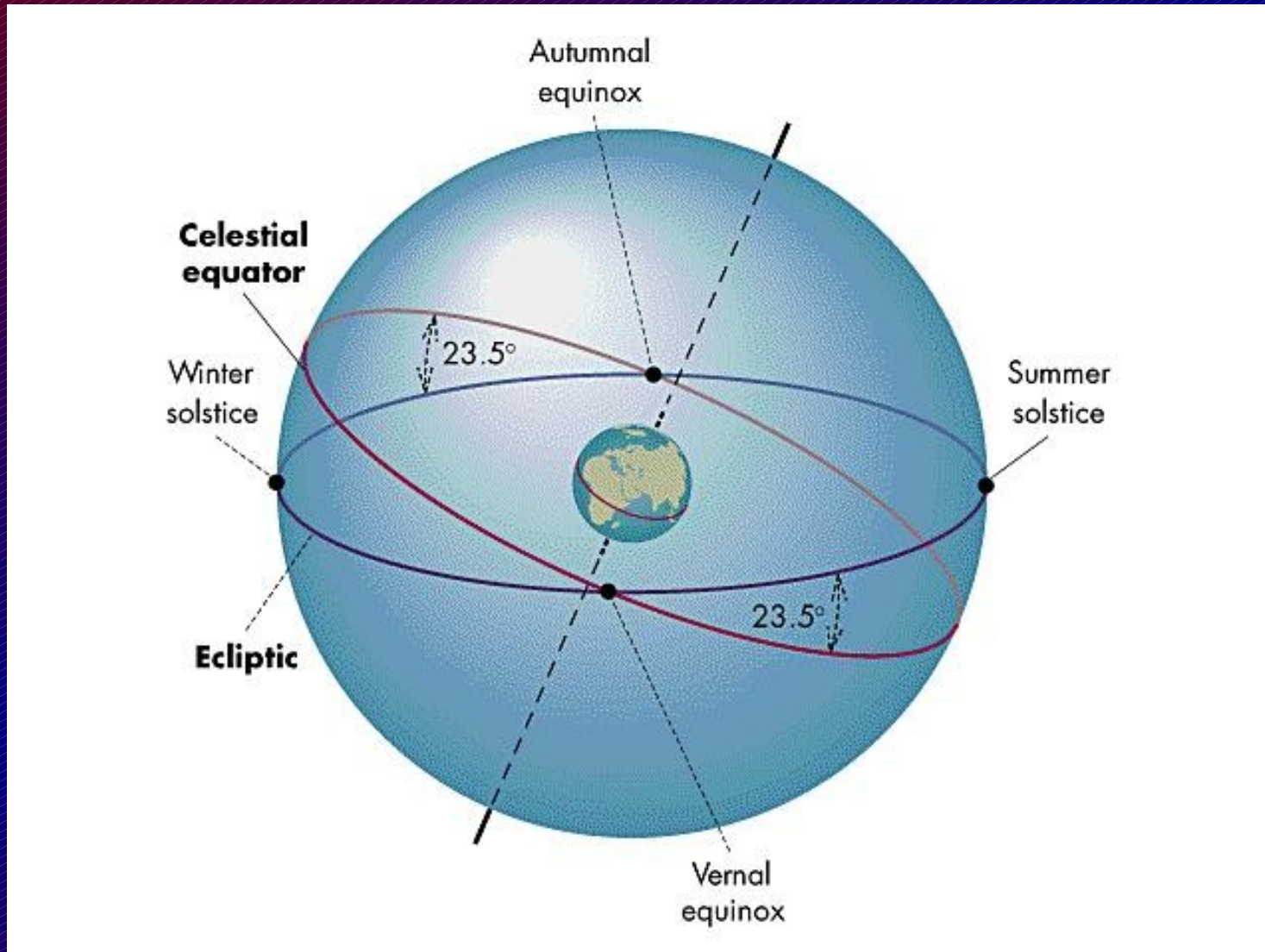
*Equatorial  
Coordinate  
System*

*Declination  
DEC or  $\delta$*

*Right Ascension  
RA or  $\alpha$*

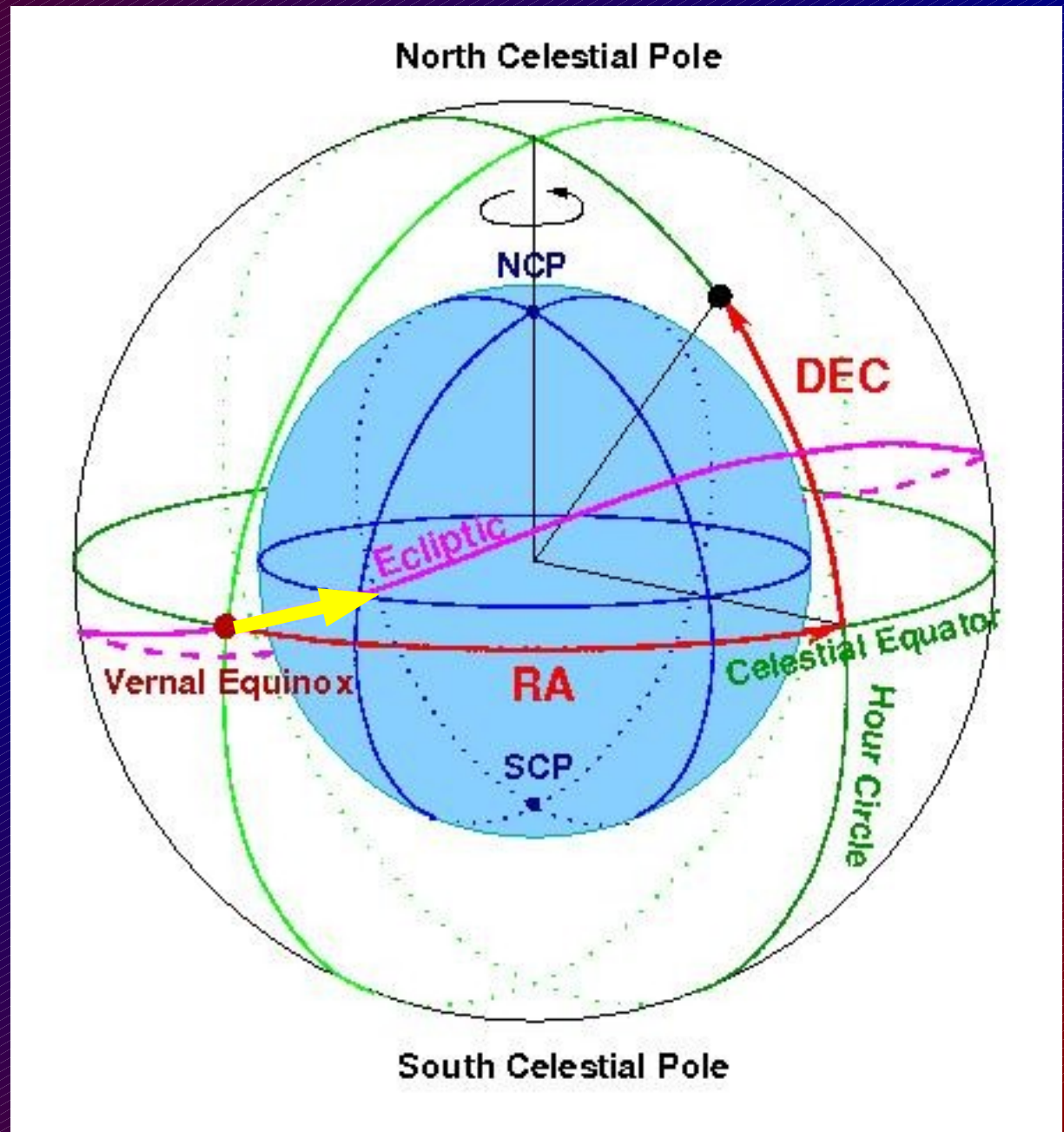


*Ecliptic in Equatorial Coordinates*

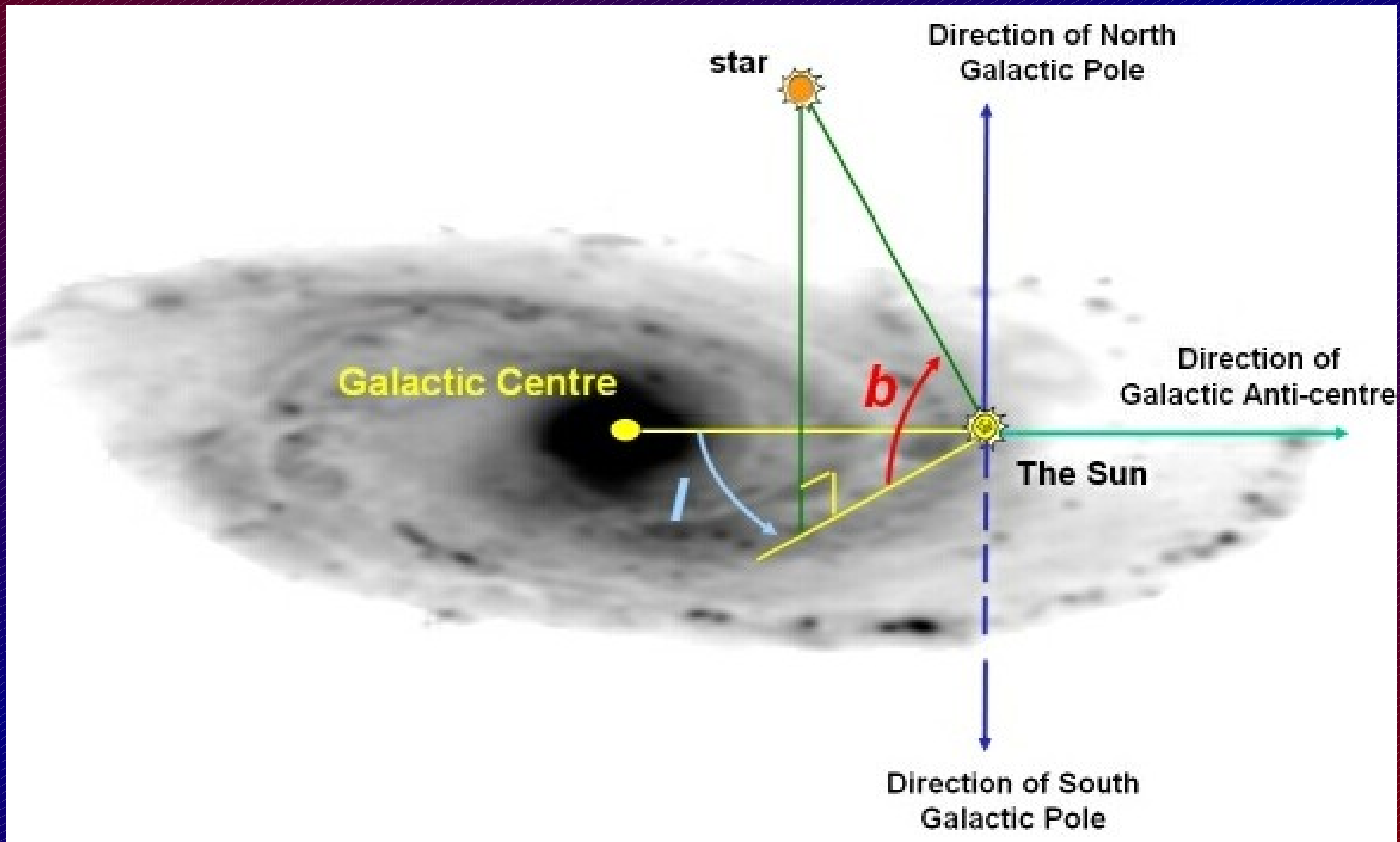


*Does Sun move in the direction of increasing or decreasing RA?*

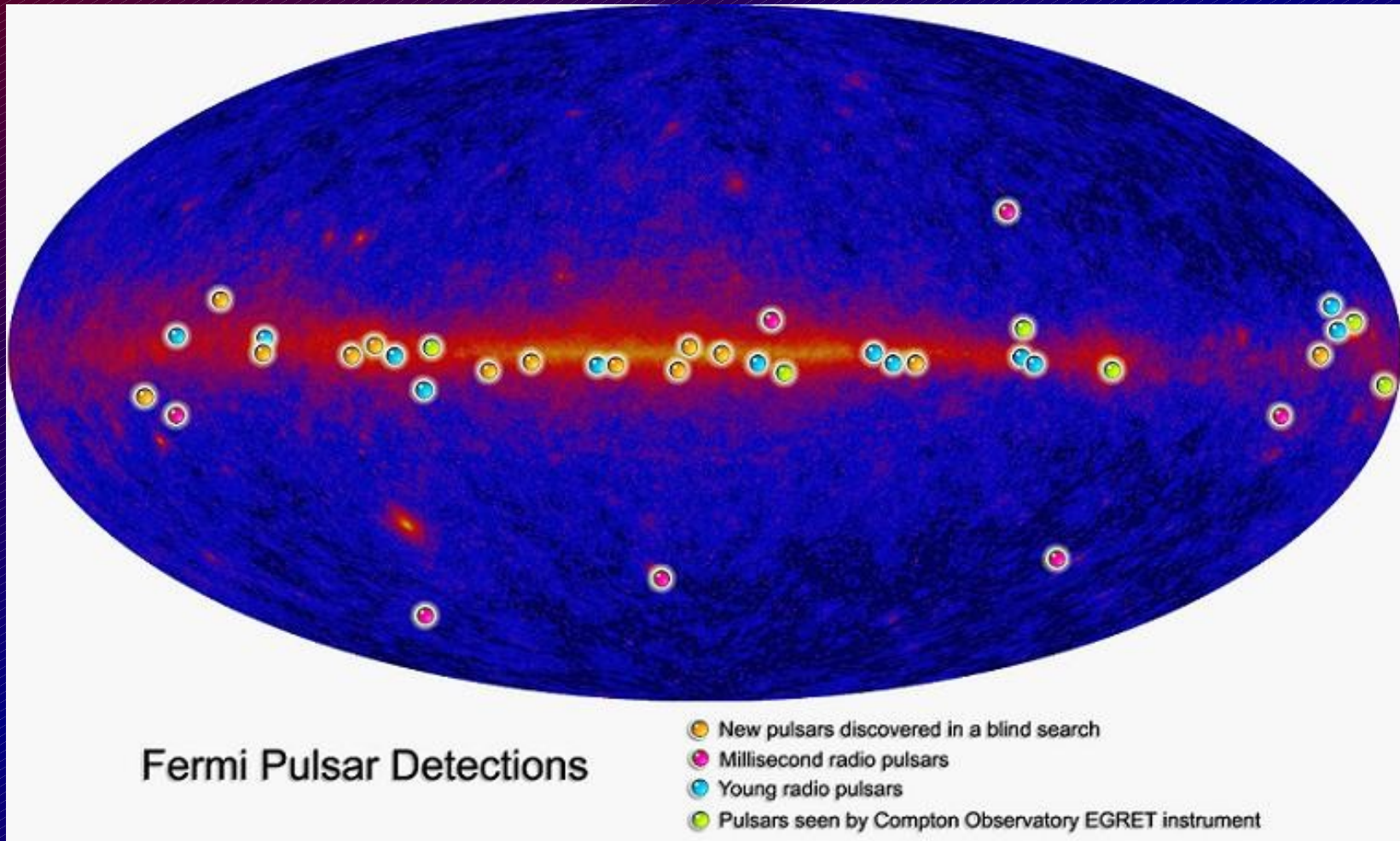
*Increasing RA*



# Galactic Coordinate System



*Galactic Coordinate System*

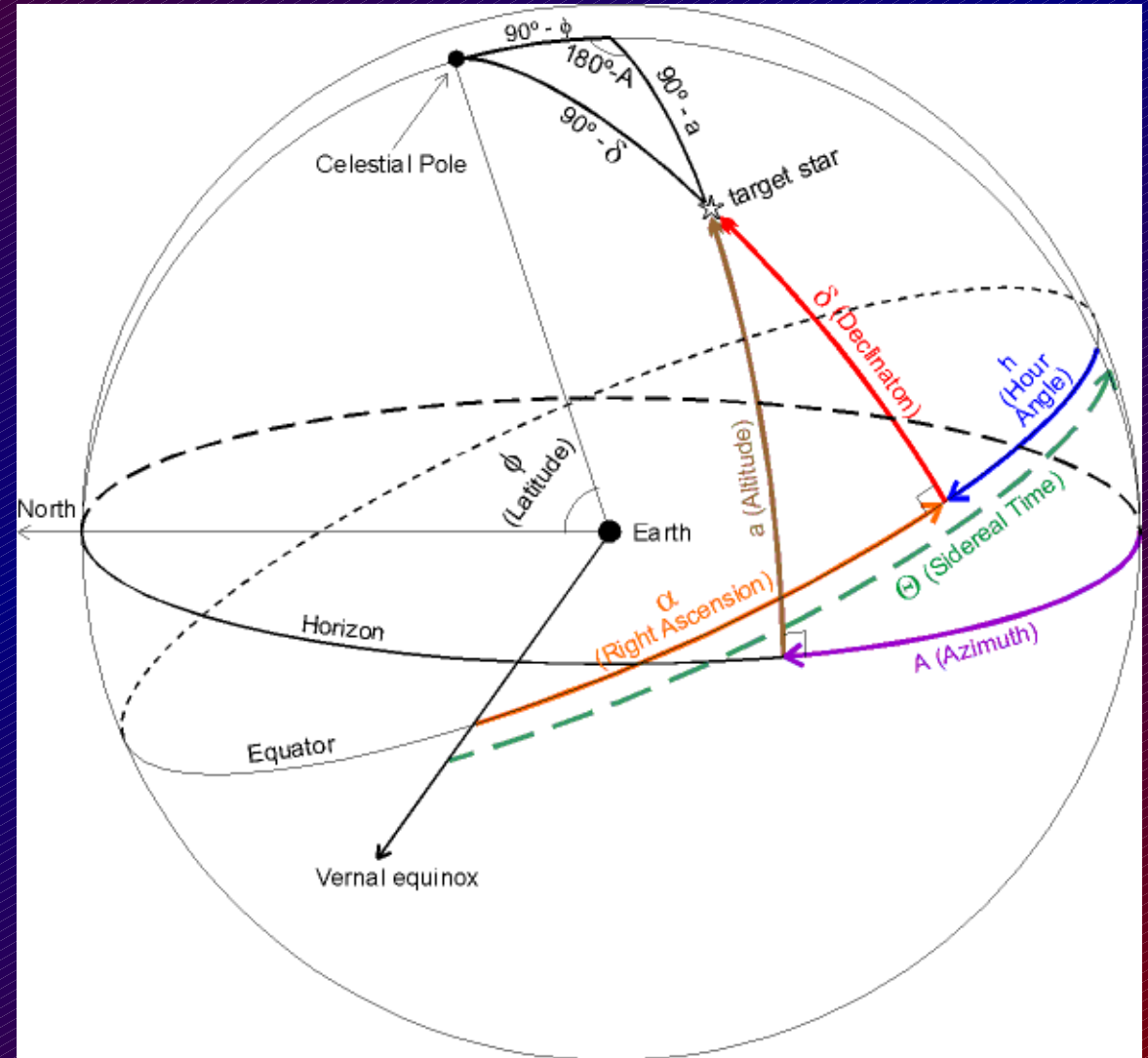


Hour Angle (HA) is measured westward from the observer's Meridian. It is analogous to RA.

HA = 0 on the meridian

HA < 0 E of meridian

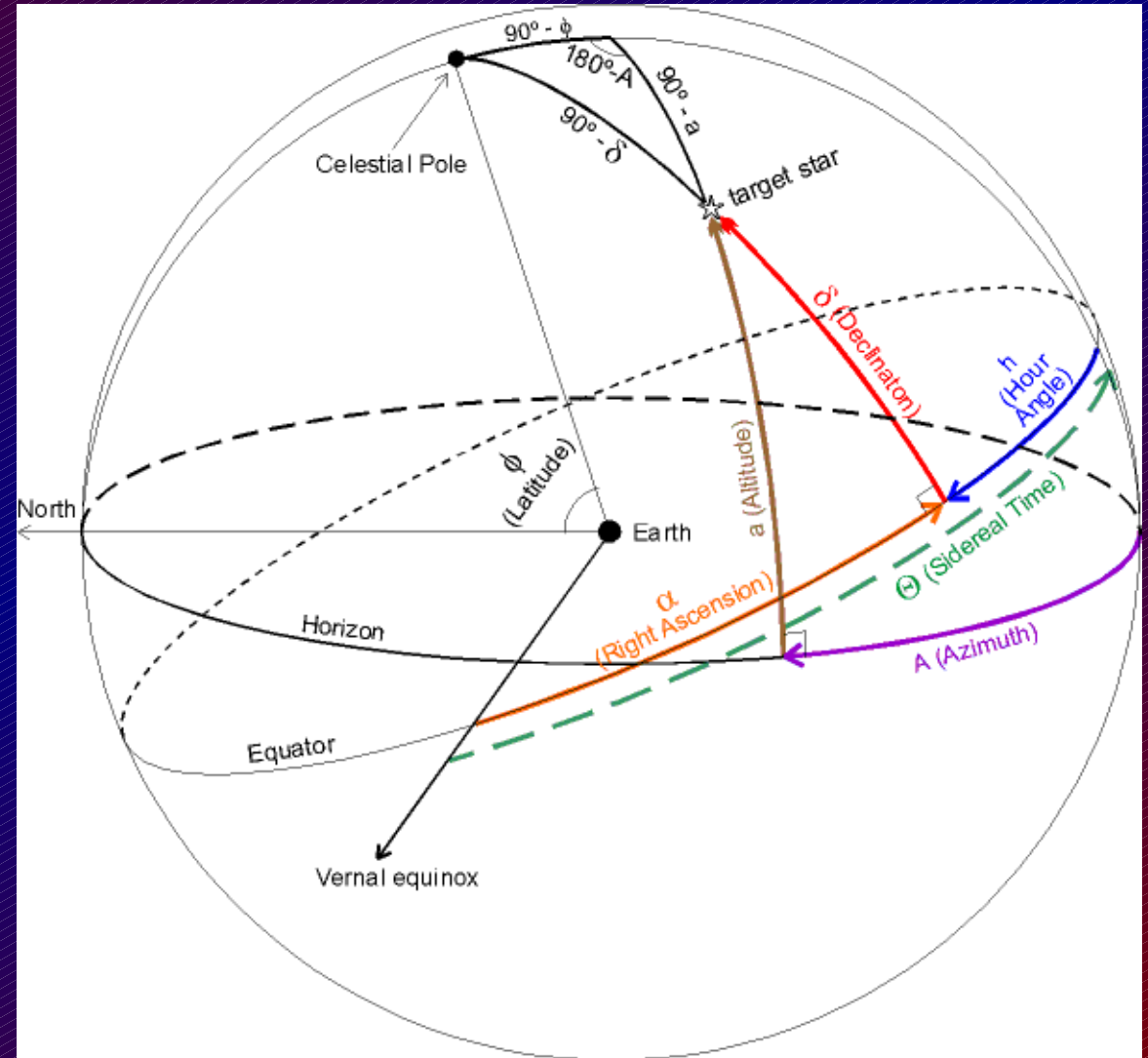
HA > 0 W of meridian



## Horizon to Equatorial Coordinate Transformation

Equivalent to a rotation by angle  $(90^\circ - \phi)$ .

$\phi$  = latitude of observer



## *Ecliptic to Equatorial Coordinate Transformation*

$$\cos DEC \cdot \sin HA = \cos alt \cdot \sin az$$

1. *(alt, az) to (HA, DEC)*

$$\cos DEC \cdot \cos HA = \cos \phi \cdot \sin alt + \sin \phi \cdot \cos alt \cdot \cos az$$

$$\sin DEC = \sin \phi \cdot \sin alt + \cos \phi \cdot \cos alt \cdot \cos az$$

2. *(HA, DEC) to (alt, az)*

$$\cos alt \cdot \cos az = -\cos \phi \cdot \sin DEC + \sin \phi \cdot \cos DEC \cdot \cos HA$$

$$\sin alt = \sin \phi \cdot \sin DEC + \cos \phi \cdot \cos DEC \cdot \cos HA$$

## Galactic to Equatorial Coordinate Transformation

$$\cos b \cdot \cos(l - 33^\circ) = \cos DEC \cdot \cos(RA - 282.25^\circ)$$

### 1. $(l, b)$ to $(RA, DEC)$

$$\begin{aligned}\cos DEC \cdot \sin(RA - 282.25^\circ) &= \cos b \cdot \sin(l - 33^\circ) \cdot \cos 62.6^\circ - \sin b \cdot \sin 62.6^\circ \\ \sin DEC &= \cos b \cdot \sin(l - 33^\circ) \cdot \sin 62.6^\circ + \sin b \cdot \cos 62.6^\circ\end{aligned}$$

### 2. $(RA, DEC)$ to $(l, b)$

$$\begin{aligned}\cos b \sin(l - 33^\circ) &= \cos DEC \cdot \sin(RA - 282.5^\circ) \cdot \cos 62.6^\circ + \sin DEC \cdot \sin 62.6^\circ \\ \sin b &= \sin DEC \cdot \cos 62.6^\circ - \cos DEC \cdot \sin(RA - 282.5^\circ) \cdot \sin 62.6^\circ\end{aligned}$$

## **Hipparcos Space Astrometry Mission**

*Launch: August 1989*

*Terminated: August 1993*

*Hipparcos Catalog (1996):*

*120,000 stars*

*1 milliarcsec*

*Tycho Catalog (1996):*

*1 million stars*

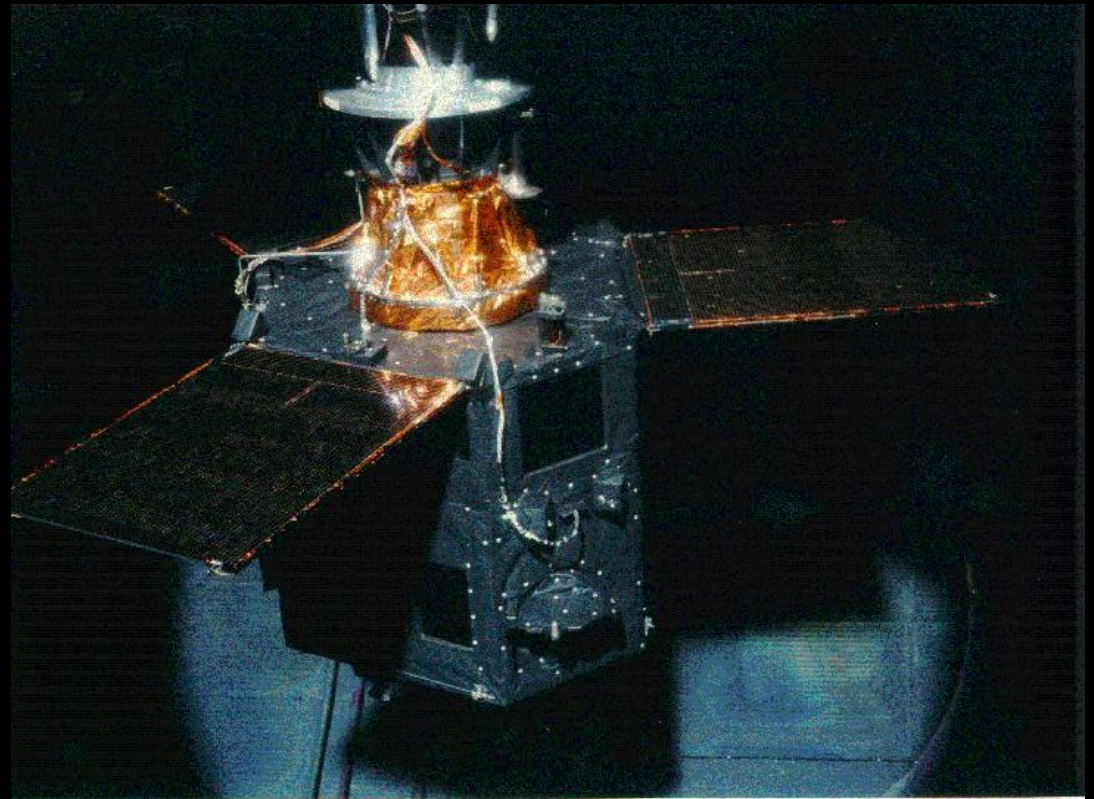
*20-30 milliarcsec*

*2 colors*

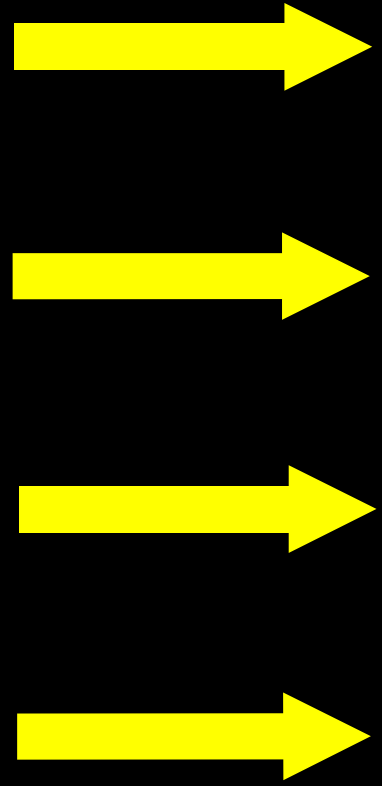
*Tycho-2 Catalog (2000):*

*2.5 million stars*

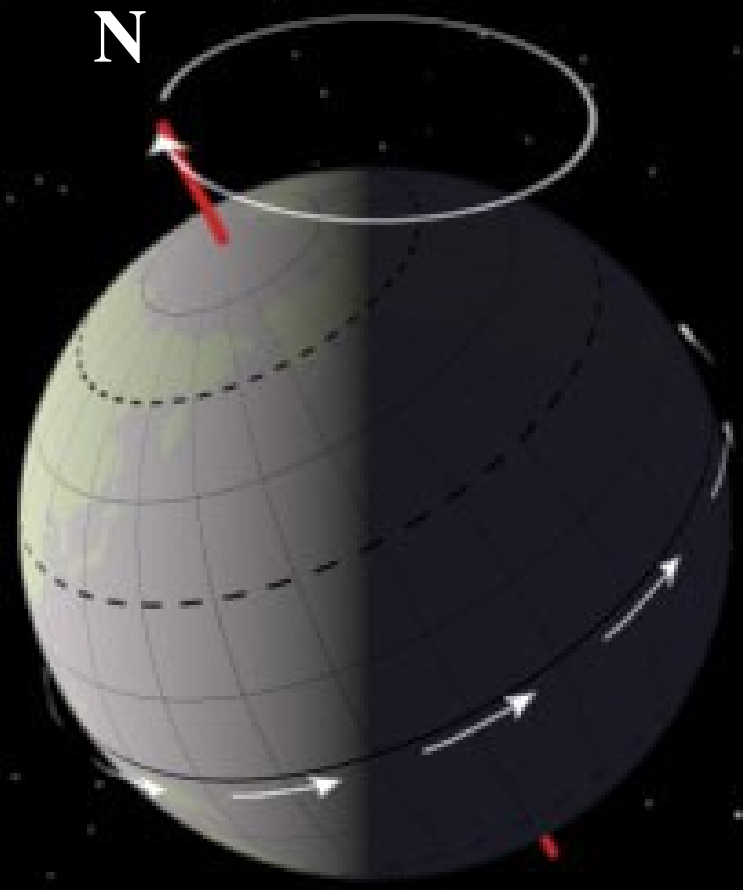
*2 colors*



**Sun**



Precession



Period = 25,750 years

*Correcting for Precession*

$$\alpha = \alpha_0 + T \theta (\cos \epsilon + \sin \epsilon \sin \alpha_0 \tan \delta_0)$$

$$\delta = \delta_0 + T \theta \sin \epsilon \cos \alpha_0$$

*$(\alpha_0, \delta_0)$  are coordinates at some epoch  $\mathcal{E}$*

*$(\alpha, \delta)$  are coordinates at epoch  $\mathcal{E}_0 + T$*

*$T$  is measured in years*

*$\theta = 50.29'' \text{ yr}^{-1}$  is the precession rate*

*$\epsilon = 23^\circ 27' 8''$  is the obliquity of the ecliptic*

*Atmospheric Refraction*



*Shift is less than 1" if  $z < 60^\circ$*